

Upconversion Luminescence of Er³⁺ and Co-Doped Er³⁺/Yb³⁺ Novel Transparent Oxyfluoride Glasses and Glass Ceramics: Spectral and Structural Properties

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Abstract: Transparent oxyfluoride silicate precursor glasses and glass ceramics with the novel composition (1) SiO₂-PbO-PbF₂-Er₂O₃, (2) SiO₂-GeO₂-PbO-PbF₂-Er₂O₃ (3) SiO₂-Al₂O₃-Y₂O₃-Na₂O-NaF-LiF-Er₂O₃-YbF₃ doped with Er³⁺ and co-doped with Er³⁺/Yb³⁺ ions were synthesized. X-ray diffraction analysis (XRD) and Er³⁺ absorption spectra revealed precipitation of PbF₂ nanocrystals dispersed in the glassy matrix. Under 980 nm laser excitation, intense green, red and near IR bands of upconversion luminescence (UCL) were recorded both before and after heat treatment. In the glass ceramics the upconversion intensity increased significantly. To our knowledge, for the first time the composition of the glass ceramics characterized by the small-angle neutron scattering (SANS) showed the cluster organization of PbF₂ nanocrystals.

Key words: Visible to near-infrared upconversion, rare-earth luminescence, oxyfluoride glass ceramics, small-angle neutron scattering.

1. Introduction

Development of high-techs claims production of stable, energy-conserving and eco-friendly equipment. One of such techniques in optics is based on the upconversion effect. The basic ideas on upconversion were generated more than 50 years ago in papers by Bloembergen and Auzel [1-3]. Later, for several decades this process, which is actually an anti-Stokes type of radiation, was widely studied by many authors and had several important applications among which are shortwave lasers, various opto-electronic devices, biophosphors, etc. [4-10]. To date the interest to the

phenomenon of upconversion has received a new impulse due to the synthesis of modern matrix elements that contain various nanocomposites.

Upconversion is most effective in doping of optically inert matrices with lanthanide ions. Fluorides, bromides, chlorides, iodides and other materials are most often used as glass matrices with low-phonon energy environment. Such environment prevents non-radiative losses of energy in the excited states of lanthanide dopants. Oxyfluoride glasses and based on them nanoceramics, that combine benefits of low-phonon energy of fluorides, chemical durability and mechanical stability of oxides, and high optical quality of silicate glasses are of special interest [11-14].

In present work, three oxyfluoride glasses with different composition of matrices were chosen for

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studies of UCL: two of them were doped with Er^{3+} ions only, and one sample was co-doped with the pair Er^{3+}/Yb^{3+} .

2. Experiments

2.1 Samples

Glass matrices doped with Er³⁺ and Yb³⁺ ions were synthesized on the basis of two oxifluoride glass-forming low-melting systems:

- (1) SiO₂-PbO-PbF₂-Er₂O₃;
- (2) SiO₂-GeO₂-PbO-PbF₂-Er₂O₃ and one hard-melting system;
 - (3) SiO₂-Al₂O₃-Y₂O₃-Na₂O-NaF-LiF-Er₂O₃-YbF₃.

The synthesis of the low-melting glass matrices was performed at 950 °C for 30 min in an electric silit furnace, and the synthesis of the high-melting matrix was done at 1,450 °C for 1 h in a gaseous open-flame furnace in corundum crucibles of 25 mL capacity in the atmosphere. The glasses obtained were annealed to relieve inner stresses. Flat-parallel polished samples of 1-2 mm thick were produced from the annealed glasses. The samples (1) and (2) were doped with the content of 1 mol% of Er_2O_3 (4.4 × 10^{20} cm⁻³), and the sample (3) was doped with 0.3 mol% of Er_2O_3 (1.48 × 10^{20} cm⁻³) and 4.3 mol% of Er_2O_3 (9.84 × Er_2O_3 (1.48 × Er_2O_3) and 4.3 mol% of Er_2O_3 (9.84 × Er_2O_3).

Nanosize oxyfluoride glass ceramics doped with ${\rm Er}^{3+}$ ions (samples 1 and 2) have been obtained on heat treatment of their precursor glasses at the glass transition temperature ${\rm T_g}$. Heat treatment was performed at 350 °C from 5 to 40 h. The composition of the crystalline phase of PbF₂ was characterized by XRD results performed at the diffractometer D8 Advance, Bruker, according to the American X-ray card-index [15].

2.2 Setups

The upconversion luminescence was studied at the multimodal optical platform "CARS" (Fig. 1).

This platform has been developed for research in microscopy and spectroscopy of spontaneous Raman scattering and its nonlinear modification known as Coherent Anti-Stokes Raman Scattering (CARS). A detailed description of the platform can be found elsewhere [16, 17]. We used the opportunity to register the medium response to the IR laser excitation in the anti-Stokes region of the spectrum for UCL studies. Excitation was provided by a continuously tunable between 690-990 nm laser delivering 6 ps pulses at a repetition rate of 85 MHz and high spectral resolution of 3-5 cm⁻¹ in the whole tuning range (model EKSPLA PT257-SOPO, Lithuania). The laser beam was focused into the sample by means of a 40× microscope objective lens with a numerical aperture of 0.6. The UCL spectra was analyzed with the monochromator-spectrograph MS-5004i and CCD camera.

2.3 Small Angle Neutron Scattering (SANS) Spectrometer YuMO

Small angle neutron scattering is a method of structural analysis of condensed matter with low space resolution by measurement and analysis of dependence of intensity of the coherent elastic scattered radiation on the scattering vector [18, 19]. The range of the values of the scattering vectors modules corresponds to the sizes of structural elements from fractions to hundreds of nanometers. The essential SANS feature is a non-destructive analysis of the inner structure of disordered systems. Its application is often the only way to obtain information about the structure of samples with chaotic



Fig. 1 Multimodal optical platform "CARS".

arrangement of inhomogeneities in the nano-size range [20].

SANS experiments were performed at the YuMO spectrometer (Fig. 2) of the IBR-2 pulsed reactor of the Joint Institute for Nuclear Research (JINR) [21, 22]. The diameter of the neutron beam can be varied from 8 to 22 mm with the intensity of up to 2.6×10^7 neutrons. The neutron flux scattered on the sample (8) comes into the vacuum neutron guide with ring detectors and direct beam detector. Monitoring and the control of the spectrometer parameters were carried out with the software SONIX [23]. Primary experimental data processing was done with the software package SAS [24, 25].

3. Results and Discussion

3.1 XRD and SANS Structural Investigations

X-ray diffraction analyses evidenced the lead fluoride PbF_2 nanocrystals precipitated in the glassy matrix of the (1) and (2) heat-treated samples. Fig. 3 shows the XRD curve of the glass ceramic: diffraction peaks exactly corresponds to the PbF_2 crystal lattice [14]. The diffraction patterns of the both heat-treated glasses (1) and (2) are identical.

The use of Scherrer equation enabled the mean size of PbF_2 nanocrystals to be evaluated about 9-10 nm in diameter.

The following mechanism of forming a nanocrystal phase of the lead fluoride in the glassy matrix can be expected: in the process of glass melting phase separation occurs in the melt. One of the phases is enriched with the lead fluoride. In the process of heat treatment, crystallization centers are generated on the border of phase separation; a crystal phase, the lead fluoride in this case, is formed and evolved around these centers with the growth of temperature and duration of the heat treatment. Trivalent ions of erbium embedded into the crystal lattice of the lead fluoride PbF₂:Er³⁺.

The XRD data accord well with the SANS results. Fig. 4 shows normalized SANS curves of samples (1)

and (2) before and after heat treatment (scattering in the sample absence was used as background).

The red curve corresponds to the glass ceramic, and the black curve to the precursor glass.

It can be definitely seen that the SANS curves for the precursor and the glass ceramic differ that indicates structural changes in glassy matrix after the heat-treating. In order to construct 3D model (ab initio model) of the nanocrystalline structure shape we used the software package ATSAS [26] and the SANS curves for the glass ceramic samples where their precursors were used as the background (Fig. 5). It leads to eliminate scattering both from the matrix itself and a non-coherent component as well.

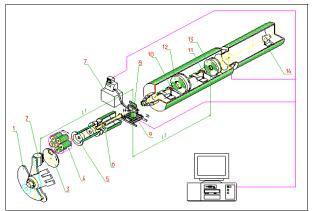


Fig. 2 Layout of the YuMO spectrometer.

(1) two reflectors; (2) moderator zone of the reactor; (3) chopper; (4) and (6) the first and the second collimators; (5) vacuum tube; (7) thermostat; (8) thermostat cassette with samples; (9) samples' table; (10, 11) Vn standards; (12) first ring-wire detector; (13) second ring detector, (14) direct beam detector.

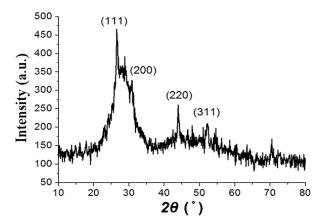


Fig. 3 The XRD curve of glass ceramic, Sample 1.

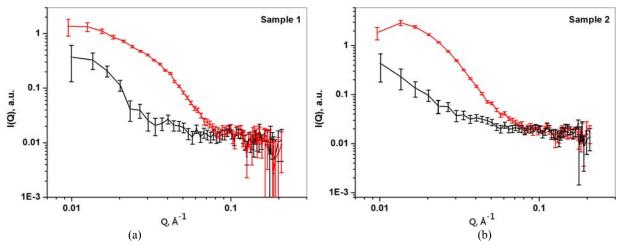


Fig. 4 SANS curves for (a) Sample 1 and (b) Sample 2.

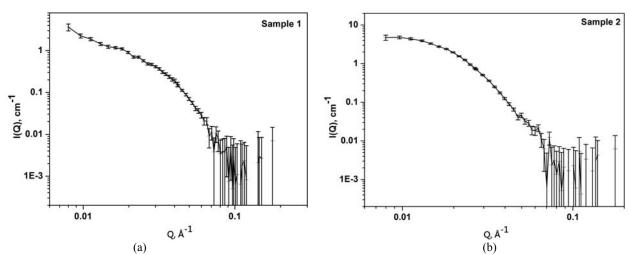


Fig. 5 Differential cross section of scattering versus the value of the scattering vector module: (a) Sample 1 and (b) Sample 2.

Figs. 6 and 7 present the projection patterns of the obtained models of the PbF_2 nanocrystals shapes for Samples (1) and (2), respectively.

As a result of modeling, the sizes and shape of the nano-scaled structures of oxyfluoride glass ceramics evidenced to the cluster pattern organization of PbF_2 nanocrystals. The sizes for sample (1) are about 10 nm in cross section that coincides to the sizes of nanocrystals assessed by XRD, and 30 nm in the longitudinal direction. Proceeding from it we can presuppose that the clusters consist of 3-4 nanocrystals.

The PbF_2 cluster concentration in samples was calculated, assuming that neutron scattering occurs in PbF_2 clusters:

$$c = \frac{I_0}{\left(\Delta\rho\right)^2 \cdot V^2}$$

where, I_0 is the intensity in zero angle, $\Delta \rho$ is the difference of neutron scattering length densities of the matrix and PbF₂ clusters (contrast), V is the cluster volume.

The data are summarized in Table 1.

For the calculation we used the values of cluster volumes and scattering intensity at the zero angles that the ATSAS software package gives.

3.2 Absorption and Upconversion Luminescence Spectra

Absorption spectra were measured at the spectrophotometer Varian Cary 5000. Fig. 8 illustrates

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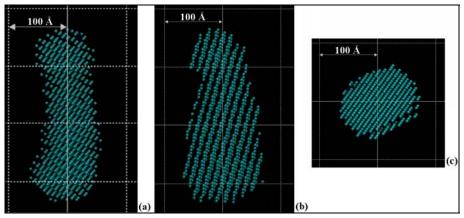


Fig. 6 Modeling results for sample (1): a, b, c, front, side and top views respectively.

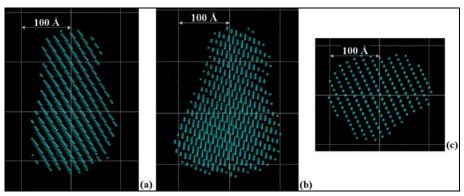


Fig. 7 Modeling results for sample (2): a, b, c – front, side and back views respectively.

Table 1 The calculated data for PbF_2 clusters, samples (1) and (2).

Sample	$I_0 (\text{cm}^{-1})$	$\Delta \rho (\text{Å}^{-2})$	$V(\text{Å}^3)$	$c (\text{cm}^{-3})$
(1)	2.2	4.29×10^{-6}	2.42×10^{6}	2×10^{14}
(2)	6.45	4.29×10^{-6}	4.94×10^6	1.4×10^{14}

the absorption spectra of Er^{3+} ions measured over the ranges of: (a) 500-570 nm, (b) 630-700 nm and (c) 780-820 nm. Three absorption bands were recorded in the visible part of the spectrum corresponding to the transitions: ${}^4\mathrm{I}_{15/2}{\to}^2\mathrm{H}_{11/2}$ (520 nm), ${}^4\mathrm{I}_{15/2}{\to}^4\mathrm{S}_{3/2}$ (540 nm) and ${}^4\mathrm{I}_{15/2}{\to}^4\mathrm{F}_{9/2}$ (650 nm). One more spectral band was recorded in the near IR range with the maximum centered around 800 nm that corresponds to the transition ${}^4\mathrm{I}_{15/2}{\to}^4\mathrm{I}_{9/2}$. For the Sample 2, the absorption curves are similar.

Due to changes of the co-ordination environment around the Er^{3+} ions in the glass ceramic samples the outer electron shells of Er^{3+} ions are distorted. This effect reveals itself in the absorption spectra curves: the Er^{3+} ions bands for glass ceramic become

structured, and new peaks, which are more indicative for crystal matrices, appear.

Fig. 9c shows the absorption spectrum of Yb³⁺ ions (Sample 3); the transition ${}^2F_{7/2} \rightarrow {}^2F_{5/2}$ corresponds to it (peak at 976 nm). On the background of a strong absorption band of ytterbium, the Er^{3+} spectrum is vaguely distinguishable.

Fig. 10a presents the upconversion luminescence spectra of precursor samples under the excitation of a 980 nm laser beam. Fig. 10b shows the energy levels diagram of Er³⁺/Yb³⁺ ions upon which the possible upconversion mechanisms is discussed.

Three dominant mechanisms are involved in the upconversion process: ground/excited state absorption (GSA/ESA), energy transfer (ET) and cross-relaxation (CR) [7, 8]. In the case of a glass matrix doped only with the Er³⁺ ions the metastable level ⁴I_{11/2} is directly excited by 980 nm pump photon (GSA) and then further excited by a second photon to the level ⁴F_{7/2} (ESA1). Besides, in the energy transfer process, two

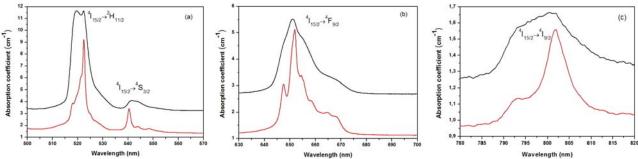


Fig. 8 Absorption spectra of sample (1) measured over the ranges of: (a) 500-570 nm, (b) 630-700 nm and (c) 780-820 nm. The black curve, precursor glass, the red curve, glass ceramics.

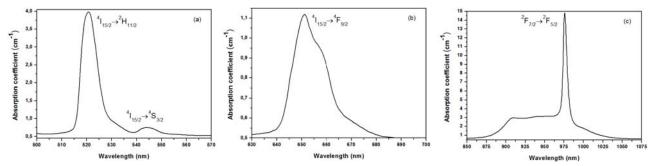


Fig. 9 Absorption spectra of sample (3) measured over the ranges of: (a) 500-570 nm, (b) 630-700 nm and (c) 850-1075 nm.

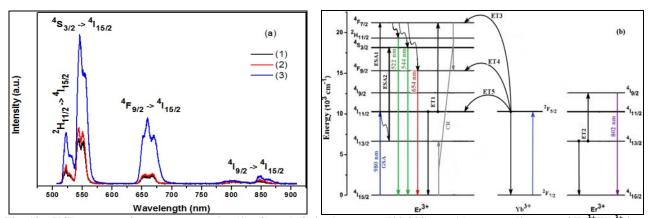


Fig. 10 UCL spectra of precursor samples (1), (2) and (3) in the range (500-900) nm (a), energy diagram of Er³⁺/Yb³⁺ ions with possible mechanisms of UCL radiation (b).

excited Er^{3+} (${}^4I_{11/2}$) ions interact with each other (ET1), thus also contribute to the population of the ${}^4F_{7/2}$ level. The UCL process can be accomplished by the non-radiative relaxations to the levels ${}^2H_{11/2}$, ${}^4S_{3/2}$, ${}^4F_{9/2}$ and further yield of three UC emissions ascribed to the transitions of ${}^2H_{11/2} \rightarrow {}^4I_{15/2}$ (522 nm), ${}^4S_{3/2} \rightarrow {}^4I_{15/2}$ (544 nm) and ${}^4F_{9/2} \rightarrow {}^4I_{15/2}$ (654 nm) respectively. The intensity ratio of green luminescence over red one is about 4 times. This can be assigned to the contribution of the ESA2 process to the population of ${}^4S_{3/2}$ level. We also recorded one more UCL band

for the all precursor glasses in the near IR range with the peaks around 802 nm and 850 nm (Fig. 10a). We consider the ET2 process as responsible for this emission band.

As for the Sample (3) co-doped with Er^{3+}/Yb^3 ions it has already been clarified that the visible UCL emission under 970-980 nm excitation mainly result from resonant energy transfer between Yb^{3+} and Er^{3+} ions [e.g., 11 and references within]. The laser pump at about 980 nm occurs mostly into absorption band ${}^2F_{7/2} \rightarrow {}^2F_{5/2}$ of Yb^{3+} (Fig. 10b) as the absorption

cross-section of the Yb^{3+} band is several times stronger than ${}^4I_{15/2} \rightarrow {}^4I_{11/2}$ of Er^{3+} ions. Besides, the concentration of Yb^{3+} ions in Sample 3 is much larger than of Er^{3+} ions. It is evident that intensity of the UCL emission for this precursor sample is relatively stronger (blue curve in Fig. 10a).

Brief summary relative to precursor glasses: novel composition of transparent oxyfluoride precursor glasses studied for upconversion emission under 980 nm laser excitation showed sufficiently intense quantum yields of UCL in the visible and near IR range of spectra.

Finally, we present our impressive results on UCL spectra for glass ceramics. For a comparison, in Fig. 11 the UCL spectra are presented for silicate (Sample 1) and silico-germanate (Sample 2) oxifluoride glasses before and after their heat treatment at temperature 350 °C for 25 and 10 h, respectively. One can see that the emission intensities in glass ceramic increases: by factor of ~7 and ~40 in

green and red bands respectively for the Sample 1, and significantly increases by factor of 25 (green) and \sim 150 (red) times for the Sample 2.

The UCL emission intensity rise in glass ceramics is due to the PbF₂ nanocrystals precipitated in the glassy matrix and can be characterized by the following factors: an interionic interactions of Er3+ ions which are mainly concentrated in the crystal lattice of PbF₂ followed by efficient near resonant cross-relaxation (CR) process [27]. This process with participation of the pair Er^{3+} - Er^{3+} (${}^4F_{7/2}$, ${}^4I_{15/2} \rightarrow {}^4F_{9/2}$, ${}^4I_{13/2}$) is depicted in (Fig. 10b). As a result, the level ⁴F_{9/2} is largely populated from level ⁴F_{7/2} that leads to intensive red radiation. Secondly, by a much lower phonon energy of co-ordination environment around Er³⁺ ions in PbF₂ glass ceramic coupled to the phonon mode at ~250 cm⁻¹ in comparison with that of precursor glasses (~1,000 cm⁻¹) [28]. Thus, the combination of above mentioned factors favor efficient upconversion emission of glass ceramic.

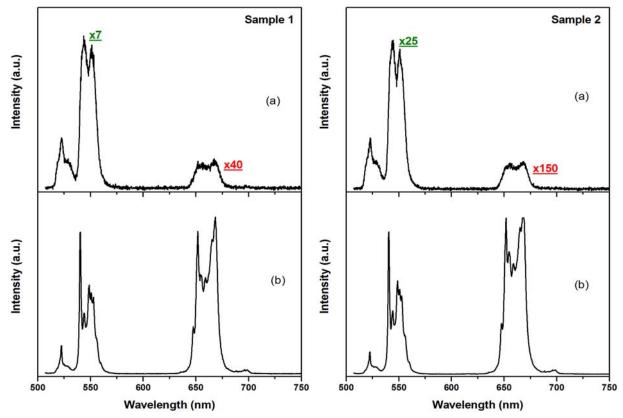


Fig. 11 UCL spectra of samples 1 and 2: (a) precursors and (b) glass ceramic.

4. Conclusions

We have developed a novel composition of transparent oxyfluoride silicate glasses and glass ceramics doped with ${\rm Er^{3+}}$ or ${\rm Er^{3+}/Yb^{3+}}$ ions. Precursor glasses display themselves sufficient intense upconversion emission in green, red and near IR ranges of spectra. Dramatic rise of UCL intensity by factor of ~ 150 was recorded for glass ceramic. To our knowledge, for the first time the structural features of glass ceramics characterized by the small-angle neutron scattering (SANS) showed the cluster organization of PbF2 nanocrystals. Obtained results may be implemented for enhancement of quantum efficiency of various UC-based devices.

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